

Bayesian Optimization for Automatic Configuration of Convolutional Neural Networks for Text Classification

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#### Abstract

Convolutional neural networks (CNNs) can be a very elective and straightforward method for performing text classication tasks, mostly because feature engineering and feature extraction are completely taken care of by the network itself. However, global optimization of expensive black-box models, such as neural networks, is a very complex task that is highly unlikely to be solved by hand. The many different parameters that have to be configured lead to high dimensionality and heterogeneity of the search space and make the problem very different cult. The black-box nature of neural networks makes that the quality of a specific configuration can only be determined empirically (i.e., by training the network and evaluating the performance), which is a very time-consuming process. In this work, we adopt a framework for Bayesian Optimization (MiP-EGO) to automatically configure CNNs for binary text classication. To this end, we introduce a simple, configurable model (TXT-CNN) that achieves state-of-the-art performances after (automated) optimization with MiP-EGO. Furthermore, the original MiP-EGO algorithm is extended to allow asynchronous execution of parallel processes running on different GPUs to obtain maximal optimization eleciency.

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# 1 Introduction

The availability of digital documents and other forms of (unstructured) textual data has been increasing rapidly with the growth of the World Wide Web over the last few decades. Much of this data is user-generated content that typically lacks a pre-de ned data model, examples being web blogs, e-mails or customer reviews. One way of organizing this kind of data is to automatically assign them to one or more pre-de ned classes (i.e. text classi cation). In this work we focus on sentiment analysis of movie reviews, an application of text classi cation where movie reviews are categorized as having either positive or negative sentiment [1, 2]. Text classi cation is an important and well-studied task on the border of information retrieval and machine learning, and many di erent approaches exist for solving this task [3]. Traditional techniques applied to this problem include Naive Bayes classi cation and Support Vector Machines [4, 5, 6]. In order to successfully apply such techniques to text, tedious feature engineering and selection are very important [7]. Recently, several papers have been published that involve convolutional neural networks (CNNs) for performing text classi cation without the need for manual feature engineering that achieved very promising results [8, 9].

Neural networks are widely used in (supervised) machine learning, for example for performing image classication tasks. With the rise of GPUs, deep learning software packages and well-established architectures like CNNs and RNNs, they are relatively easy to use and often provide more than satisfactory results. One of the most often praised properties of neural networks is their ability to automatically extract features from data, thus removing the need of manual feature engineering as in traditional techniques (e.g. Naive Bayes, Support Vector Machines). However, practitioners are still stuck with the task of designing the network architecture and selecting many speci c parameters, which can be a very tedious job. The most straightforward approach is performing a grid-search: de ning a grid of parameters with pre-de ned value ranges, exhaustively changing one parameter at a time while keeping the others static in order to nd the best performing model. The problem of such an approach is the high probability of getting stuck in a local optimum, and it has even been shown that a random search might perform better than a grid search for hyperparameter tuning of machine learning models [10]. More sophisticated methods are thus needed for optimizing neural network architecture and hyperparameter con quration.

In this work, we adopt a Bayesian Optimization approach for e ciently optimizing CNN architecture and hyperparameters for text classi cation. To that end, we use an adapted version of the popularE cient Global Optimization (EGO) algorithm [11], which we will refer to as Mixed-integer Parallel EGO (MiP-EGO) [12]. The original EGO-algorithm has been developed for the optimization of expensive black-box functions. Examples of such functions are geographically determining location sites for oil drilling, measuring drug e ectiveness in clinical trials and nding neural network performance where network training often takes long.

In this paper, we introduce a con gurable model (TXT-CNN) and apply MiP-EGO to it for automatic con guration and optimization. Furthermore, the original MiP-EGO algorithm was extended to allow asynchronous execution of parallel processes running on di erent GPUs in order to obtain maximal e ciency during optimization (this is described in more detail in section 4). We test the algorithm under di erent setups on our dataset and compare the results of the found (sub)optimal solutions to networks that were tuned using grid-searches.

#### 1.1 Problem statement

The problem of optimizing the architecture and hyperparameter con guration of a convolutional neural network can be stated concisely as

$$\max_{x \ge S} f(x) \tag{1}$$

That is, we want to optimize the performance of our network (a non-linear function f that has as input a parameter con guration x) for all possible combinations of parameter con gurations S. This is a complex task for several reasons. First, the black-box nature of neural networks in general makes it impossible to do a manual or intuition-based search: the performance of a speci c con gurationx can only be determined empirically. Second, training times for CNNs are relatively long even when using GPUs (especially when using much data), making (semi-)exhaustive approaches like grid search even more obsolete. Third and last, the search space for this task is very complex. The number of parameters to be set for con guring CNNs can be very big and heterogeneous, leading to high dimensionality and heterogeneity of the search space. Also, we often have to deal with conditional variables that only make sense in combination with other variables.

## 1.2 Report outline

The remainder of this report is organized as follows. First, we introduce neural networks in section 2.1. In particular, we discuss CNNs for text classi cation in subsection 2.1.2. Next, we cover the principles of Bayesian Optimization in section 2.2. We then look at related work in the eld of automatic parameter con guration in section 2.3 and explain how MiP-EGO works in section 3. In section 4 we discuss how we extended the original MiP-EGO algorithm. Next, in section 5 we introduce our dataset, present our con gurable CNN model for text classi cation (TXT-CNN) and discuss the experimental setup. We then present our results in section 6, followed by a discussion and conclusion in section 7.

# 2 Background and Related Research

### 2.1 Background: Neural Networks

Neural networks (NNs) are machine learning methods that are inspired by the functioning and architecture of biological nervous systems, such as the human brain [13]. They consist of many interconnected neurons, usually distributed over multiple layers, that work together to solve complex tasks [14]. The distributed arrangement of their neurons allows NNs to perform massively parallel computations when learning from the input data. Furthermore, by applying nonlinear functions to their neurons, NNs are able to learn and successfully classify non-linearly separable data without losing generalization ability of the model [15].

A brief history of NNs The birth of NNs dates back all the way to 1958, when Rosenblatt introduced the perceptron [16]. After the publication of the backpropagation algorithm for training multilayer perceptrons NNs gained much popularity [17], leading to the development of Convolutional and Recurrent Neural Networks (CNNs and RNNs). However, the AI community lost faith in NNs in the mid 90s and was mainly focused on the uprising Support Vector Machine (SVM). When Hinton et al showed that NNs could achieve better results than SVMs on the MNIST benchmark dataset in 2006 [18], excitement for NNs reemerged and ultimately led to the current machine learning revolution caused by deep learning [19]. The development of Graphics Processing Units (GPUs) for speeding up the training process of NNs has also been a very important factor for this reestablished interest.

Architecture of NNs Two examples offeed-forward NNs can be found in Figure 1: one network with 3 layers and another network consisting of 4 layers. This type of network is called feed-forward because the neurons in each layer pass on output signals to the neurons in the following layer.

Figure 1: NNs with 3 (left) and 4 (right) layers (image retrieved from http://cs231n.github.io/convolutional-networks/).

We can see how the neurons of a neural network function in Figure 2. The left side of this gure shows a biological neural network, while the right side represents its arti cial counterpart. An arti cial neuron (or node) receives input signalsx from neurons in the previous layer. In this example, the neuron receives three di erent inputs, so  $x = f x_0; x_1; x_2g$ . Furthermore, the weights  $w = f w_0; w_1; w_2g$  and a bias b are associated with the neuron. Its output y is calculated by multiplying each input  $x_i$  with weight  $w_i$  and optionally adding a bias term b, before passing the result through an activation or transfer function f:

$$y = f$$
 $\begin{cases} x^2 & ! \\ w_i x_i + b \end{cases}$ 
(2)

Popular choices for are e.g. the recti ed linear unit (f (x) = max(0; x)) or the sigmoid function ( =  $\frac{1}{1+e^{-x}}$ ).

Figure 2: The output of an arti cial neuron is computed by multiplying inputs x and weights y (and optionally the addition of a trainable bias term y b) and passing the result to an activation function y (image retrieved from http://cs231n.github.io/convolutional-networks/y).

#### 2.1.1 Convolutional Neural Networks

Convolutional Neural Networks (CNNs) are a type of feedforward networks that apply convolving Iters to local features in the input data and are often used in the eld of computer vision and object recognition [20]. As illustrated in Figure 3, the neurons in the convolutional layer of a CNN scan local regions of the input data and have shared weights across the full input. Furthermore, multiple Iters of the same size can be used to scan the same input regions but look for complementary features.

Figure 3: Schematic overview of how convolutional lters are applied to input data. The convolutions are projected onto the convolutional layer (blue volume): multiple neurons can have the same receptive eld for learning complementary features (image retrieved from http://cs231n.github.io/convolutional-networks/ ).

#### 2.1.2 CNNs for Text Classi cation

CNNs are a natural t for image classi cation tasks because their aim is to learn features locally. As pixels in images have a higher probability to originate from the same object when they are located in the same local region, we can understand why CNNs are able to achieve excellent results in the eld of computer vision and object recognition. It might be less straightforward to apply the same approach for text classi cation, but it has been shown that CNNs can achieve excellent results on tasks like sentiment analysis as well [8, 9]. We show which components are needed for applying CNNs to text and how they work in practice in the following paragraphs, followed by an introduction to word embeddings for representing words as vectors.

Sentence Matrix In order to apply convolutions to text in a similar way as they are applied to images, we need to represent the input similarly as well [21]. This is achieved by creating a sentence matrix: a matrix that represents a single sentence or document and where each row corresponds to a token or word. The row vectors have a xed length, namely the length of the embedding vectors that are used to represent words (more on word vectors in Section 2.1.2).

Convolutions In images, convolutions are typically two-dimensional: the Iters scan the input data in both the vertical and horizontal dimension, leading to a two-dimensional output. When we use a sentence matrix for representing text, however, it does not make sense to use a Iter that scans the input horizontally: as one row in the matrix represents a single word, Iters should be used that scan this word vector across its full dimensionality. The convolutional Iters that are applied to the sentence matrix have di erent heights. As Iters are of the same width as the input data, convolutions will lead to one-dimensional feature maps as output. It is common to use multiple Iters of the same size for learning complementary features from the same local input.

Pooling As di erent convolutional Iter sizes lead to feature maps of di erent lengths, pooling is applied to each feature map for extracting only the highest activation in that map. After concatenation of the resulting values the nal set of high-level features is obtained.

Regularization In order for the network to generalize well on unseen data, regularization for preventing over tting is important. One way for achieving this is by using dropout layers, where neurons are randomly set to zero (\dropped out") with dropout probability p. Another method for regularization is L2-norm constraint regularization: at each step in the training process, each node is re-scaled such thin  $\mathbf{j}_{12} = \mathbf{L}_{22}$  whenever  $\mathbf{j}_{12} = \mathbf{L}_{22}$ .

Output The feature vector that was obtained after performing the convolutions is connected to a single output neuron via a hidden layer. The output is computed by applying a sigmoid function to the linear combination of the weights and incoming activations, such that the nal output is in the range [0, 1]. The nal binary classi cation is made by using a cut-o value at 0.5.

# Word embeddings

In traditional document representation, the Bag-of-Words model is used for representing documents as vocabulary-sized feature vectors using term weights likef-idf. Such huge and sparse vectors would obviously not be a good choice to use as input for a neural network, as we apply Iters with the same dimensionality as the size of the word representation (leading to a huge number of weights). A better idea is to use word embeddings: these are vector representations of words with an arbitrary number of dimensions that can be learned in an unsupervised manner, for example using word2vec.

Word2vec Word2vec is a set of unsupervised machine learning techniques for creating word embeddings of high quality [23, 24]. This can be achieved by using either the Skip-gram model or the Continuous Bag-of-Words (CBOW) model. These models are neural networks with a single hidden layer that predict the probability of context words given a single input word, and the probability of a word given some input words, respectively. The context can take on an arbitrary sizen. The true probabilities are easily computed by

simply counting the frequencies of words that are in the same context window of any other word among all documents in the training corpus. Figure 4 shows an example network of context size 1 (and can therefore be interpreted as both CBOW and skip-gram).

Figure 4: Network architecture in word2vec for a context of size one (gure from Rong [25]).

After training these networks on some text corpus, the matricesW and W' contain vectors (of arbitrary length N, i.e. the size of the hidden layer) for every word in vocabularyV: each word is thus represented twice (once as context word and once as middle word). Combining these vectors (e.g. averaging them), we end up with the nal word embeddings.

The nal word vectors generated with word2vec carry lots of semantic information and are therefor very suited for NLP tasks. Like any neural network, word2vec-networks are black boxes that don't explicitly clarify why they work well. One intuitive explanation is that in most texts, similar words have similar context. When looking, for example, at the sentence We pointed the door \_\_\_\_\_", we expect the missing word to be fred, green, blue,..g. However, words likeyesterday would obviously the sentence as well, without sharing the desired similarity of the other words.

The authors of the original papers additionally published a set of pre-trained word embeddings. These vectors were trained with word2vec on a Google News dataset of roughly 100 billion words, which resulted in very high quality word embeddings in terms of capturing semantic relationships between words, as shown in Figure 5.

Figure 5: Because the word vectors for man and woman is are equally distant from resp. king and queen very intuitive vector calculations can be made, e.g. v(king) - v(man) + v(woman) v(queen) (image retrieved from https://www.tensor ow.org/images/linear-relationships.png ).

#### 2.2 Background: Bayesian Optimization

Bayesian Optimization is a probabilistic method for global optimization of an objective function f. The key element of Bayesian Optimization is the assumption of a prior distribution of the objective function, from which a posterior distribution is obtained and iteratively updated using Bayes' Rule as new observations of the objective function are accumulated (i.e. Bayesian inference). As opposed to local search methods, e.g. gradient descent, Bayesian Optimization methods use all observations of accumulated so far to determine the next evaluation point.

When considering machine learning models (neural networks in our work), the tness function is typically de ned as the model performance in terms of e.g. accuracy or loss. Assuming a pri $\Re(f)$  of this tness function and letting  $x_i$  represent the i'th parameter con guration of the model and  $f(x_i)$  the true tness function, we obtain the accumulated set of observation  $\mathfrak{D} = fx$ ; f(x)g. The posterior distribution can then be found via Bayesian inference as in Eq. 3.

$$P(f jD) / P(D)P(f)$$
 (3)

The meta-model P(f) is known as asurrogate model and for determining which point should be evaluated next (with the true tness function), acquisition functions are used. These components are discussed in the next sections. An overview of a generic Bayesian Optimization algorithm can be found in Algorithm 1.

#### Algorithm 1 Bayesian Optimization

- 1: Initialize  $D_t = fx_{1:t}; f(x)_{1:t}g$
- 2: Construct surrogate model with Dt
- 3: while not stopping criterion do
- 4: Select x<sub>t+1</sub> by maximizing an acquisition function M:

$$x_{t+1} = \underset{x}{arg max} M (x; D_t)$$

- 5: Evaluate  $x_{t+1}$  on the true objective function to obtain  $f(x)_{t+1}$
- 6: Augment data  $D_{t+1} = fD_t; (x_{t+1}; f(x)_{t+1})g$
- 7: Update surrogate model with D<sub>t+1</sub>
- 8: t t+1
- 9: end while

#### 2.2.1 Surrogate models

The estimate of f is thus constructed by using a nite number of samples of the true tness function, and is known as a surrogate model. Intuitively, the surrogate model will have high uncertainty in regions that are not explored yet and vice versa.

Gaussian Processes (GPs) are a very common choice to use as surrogate models for Bayesian Optimization. A GP is a stochastic process that de nes distributions over functions and is completely specified by a mean function m(x) and a covariance function (or kernel function)  $k(x; x^0)$  (see Figure 6).

f GP 
$$(m(x); k(x; x^0))$$
 (4)

Furthermore, the prior mean m(x) is often assumed to be 0 for convenience. A popular choice for the covariance function  $k(x; x^0)$  is

$$k(x; x^{0}) = \exp \frac{1}{2} jjx \quad x^{0}jj^{2}$$
 (5)

This function gets closer to 1 as points lie closer together, and approaches 0 when points get further apart. Because all variables are weighted equally in Eq. (5), an additional parameter vector is commonly introduced, where each i measures the importance and e ectively regulates the activity of variablexi, as suggested by e.g. Jonésin the original EGO algorithm [11].

By the properties of a centered Gaussian Process, we know that any nite collection of its random variables are jointly Gaussian. Given a set of observations  $D = f x_{1:t}$ ;  $f(x)_{1:t}g$ , we can thus model an arbitrary point  $x_{t+1}$  that we may want to evaluate next with the joint distribution

where k is a vector of covariance terms between  $x_{t+1}$  and  $x_{1:t}$ . The posterior distribution can then be written as

$$P(f_{t+1}|D_{t+1};X_{t+1}) = N((x_t+1);^2(x_{t+1}))$$
(7)

where

$$(x_t + 1) = k^T K^{-1} f_{1:t}$$
 (8)

$${}^{2}(x_{t+1}) = k(x_{t+1}; x_{t+1}) \quad k^{T} K^{-1} k:$$
 (9)

#### 2.2.2 Acquisition functions

Having de ned a statistical model for representing the posterior distribution of the (unknown) function f as a combination of a mean function and an uncertainty term, we now focus on methods for selecting promising candidate points that we might want to evaluate next. In Bayesian Optimization, this is typically done by using an acquisition function, or in II-criterion . In order for the algorithm to converge to a global optimum, it is important that the acquisition function carefully balances exploration of new areas with high uncertainty and exploitation of regions with high estimated function values. Here we discusprobability of improvement, expected improvementand the moment-generating function for nding the global minimum of f.

Probability of Improvement The rst acquisition function we discuss is the Probability of Improvement (PI). The function rewards solutions that may have an improved tness value over the best observation found so far (i.e., the incumbent)  $f(x^+)$ :

$$PI(x) = P(f(x) < f(x^{+}))$$
 (10)

$$= \frac{f(x^+)(x)}{(x)}$$
 (11)

<sup>&</sup>lt;sup>1</sup>Actually, Jones de nes a correlation function for expressing variable distances, which is obviously very similar to using a covariance function

Figure 6: Toy example of a one-dimensional Gaussian Process prior on a tness function f (solid black line). Four points have already been evaluated with the true tness function and have zero variance (although not perfectly visible in the gure). Every other point  $x_i$  is modeled as a Gaussian distribution with mean  $(x_i)$  and standard deviation  $(x_i)$  (gure from Brochu et al [26]).

Here, ( ) is the normal cumulative distribution function. Because the PI-function chooses to draw points that are in nitesimally smaller than the incumbent over points that may o er greater gains but with high uncertainty, this acquisition function has a highly exploitative nature.

Expected Improvement The Expected Improvement (EI) extends PI by including the magnitude of the improvement a solution can potentially yield. The improvement is de ned as

$$I(x) = \max \ 0; f(x^{+}) \ f(x) :$$
 (12)

The expected improvement is the expected value of (12) and can be expressed in closed form as

$$EI(x) = (f(x^{+}) (x)) \frac{f(x^{+}) (x)}{(x)} + (x) \frac{f(x^{+}) (x)}{(x)} (13)$$

where is the normal probability density function and the normal cumulative distribution function.

MGFI-acquisition The third and last acquisition function we discuss was proposed by Wanget al [27] and is based on the moment-generating function of the improvement (MGFI). The function takes all the higher moments into account and introduces a parameter (f) for explicitly balancing exploration and exploitation.

MGFI(x;t) = 
$$\frac{f(x)}{(x)}$$
 exp (f(x)) (x) 1)t +  $\frac{{}^{2}(x)}{2}$ t<sup>2</sup> (14)

Lower values oft assign more weight to the lower moments, leading to a more exploitative search behaviour. Conversely, higher values of lead to a more explorative search behaviour.

### 2.3 Related Research

The idea of automatic algorithm con guration is not new. As mentioned before, performing a grid search can be less e cient than a random search [10], underlining the need for more sophisticated methods for hyper-parameter optimization. Especially model-free algorithm con guration methods have been widely studied. Examples are evolutionary algorithms, F-RACE [28] (based on theracing algorithm [29]) and ParamILS [30] (based on iterated local search). A major disadvantage of these methods is that the search is guided locally, leading to a high probability of getting stuck in a local optimum.

Model-basedalgorithm con guration methods, on the other hand, use meta-models and iterate between t-ting them and using them to select new points for evaluation (i.e. Bayesian Optimization). This approach is also referred to as Sequential Model-Based Optimization (SMBO) by Hutteret al [31]. The roots of these methods are all based on the work of Jones and the introduction of the GO-algorithm [11]. Examples are ROAR (Random Online Adaptive Racing) and SMAC (Sequential Model-based Algorithm Con guration) by Hutter et al [31]. These methods have been successful in autoML tools like Auto-WEKA [32] and auto-sklearn [33].

More recently, an extension of EGO known as MiP-EGO (Mixed-integer Parallel-EGO) was introduced by Van Stein et al and applied to parameter optimization of CNNs for image classication tasks [12]. The method can handle mixed-integer data by using Random Forests as surrogate models, instead of Gaussian Processes as in traditional EGO. Furthermore, multiple candidate points can be selected and evaluated in parallel, which is extremely useful when optimizing CNNs and multiple GPUs are available for evaluating network con gurations.

### 3 MiP-EGO

MiP-EGO follows the generic Baysian Optimization framework as described in Algorithm 1. The initial set of candidate points f(x) is created using latin hypercube sampling (LHS). After evaluation of these points on the available GPUs and obtaining tness values f(x) if f(x) the initial dataset is used to the Random Forest as a surrogate model for optimization (allowing mixed-integer data). An acquisition function is then maximized for selecting the next point for evaluation (section 3.1). Currently MiP-EGO has PI, EI and MGFI (section 2.2.2) implemented. After evaluation, the set of known congurations and corresponding tness scores is augmented, the surrogate model is re-tted and the process restarts.

MiP-EGO allows for multiple candidate points to be selected and evaluated in parallel, which is an extremely useful feature that was not supported in the traditional EGO-algorithm. Selecting multiple candidate points simultaneously can be done by constructing multiple instances of the MGFI -acquisition function using di erent values for to ensure that the acquisition functions that are optimized are unique. This is implemented in MiP-EGO by using a log-normal distribution from which di erent values for to are sampled. The idea is that by using this long-tailed distribution, most values for to are small and thus well suited for exploitation, whereas few values will be large and guide the algorithm's explorative behaviour [12].

#### 3.1 Optimization

Optimization of the acquisition function is done using evolutionary algorithms. In particular, Mixed-Integer Evolution Strategies (MIES) are applied to the problem [34]: a natural extension of CMA-ES [35] for mixed-integer optimization problems. An outline of this algorithm can be found in Algorithm 2. Since we use a (; )-selection scheme, the best individuals in each generational cycle are only selected from the o spring population , ignoring the parent population P(t).

```
Algorithm 2
                      )-Evolution strategy
 1: t
         0
 2: initialize population P(t) 2 I
 3: evaluate the initial individuals with tness function f
 4: while not stopping criterion do
        for i 2 f 1; :::; g do
 5:
            randomly select parentsp<sub>i1</sub> and p<sub>i2</sub> from P(t)
 6:
                  mutate (recombine(p<sub>i1</sub>; p<sub>i2</sub>))
 7:
            Q(t)
                     Q(t) [f x_i g]
 8:
                   individuals with best tness value from Q(t)
        P(t)
 9:
        t
             t + 1
10:
```

# 4 Contribution

In this work, MiP-EGO is adopted and used for optimizing CNNs for text classi cation. Recall from section 2.1 that GPUs lead to a typical 100- to 1000-fold speedup of the training process and are therefore extremely useful for training and evaluating neural network con gurations. In the original MiP-EGO software, multiple candidate points can be selected and evaluated in parallel if multiple GPUs are available (see section 3), which is an extremely useful extension to the original EGO-algorithm. The implementation of this feature in MiP-EGO was originally such that the evaluations of all candidate points in a single MiP-EGO iteration would run synchronously on the available GPUs. Thus, before the selection of a new set of candidate points for evaluation, all evaluations of the previous set would have to nish rst (such that at the end of the optimization each GPU would have done the same number of function evaluations, see lower part of Figure 7).

Upon completion of an evaluation in the synchronous parallelization, a GPU thus has to wait on all other evaluations running in parallel to nish before getting assigned a new task. This is obviously very ine cient in terms of algorithm running time, even more so because training times of CNNs can vary substantially for di erent con gurations (depending e.g. on the number and sizes of convolutional lters). One slow evaluation among all candidate points might therefore cause all other GPUs to be idle for hours, which is simply wasted time.

To overcome this problem, we extended the original software by implementing a more e cient parallelization of the GPUs: candidate points are evaluated asynchronously by using multithreading, allowing the GPU to evaluate a new candidate point as soon as the previous evaluation is nished. This way, all GPUs are constantly working instead of having to wait for all other GPUs to nish their task rst (see upper part of Figure 7). To achieve this, we launch one thread per available GPU and use one evaluation queuethat is shared across these threads. Now every time a GPU nishes an evaluation, its thread computes a new candidate point by re- tting the surrogate model and maximizing the acquisition function on that model, adds this point to the evaluation queue and starts evaluating the rst next point in the queue. Furthermore, the surrogate model is not shared across the di erent threads, as this may cause errors when di erent threads try to t the surrogate model at the same time. We therefore make sure that each thread has its own unique copy of the surrogate model.

Figure 7: Synchronous (lower part) and asynchronous (upper part) execution of evaluations using multiple GPUs. In the asynchronous implementation, all GPUs are constantly working, while in the synchronous parallelization GPUs have to wait until all evaluations are nished before getting assigned a new job.

# 5 Dataset and experimental setup

# 5.1 Dataset

Experiments are conducted on theMR dataset: this dataset contains movie reviews from theRotten Tomatoes website<sup>2</sup>. The reviews are approximately one sentence long and were automatically labeled positive or negative, based on the review being markedresh or rotten, respectively.

The MR dataset consists of 10662 reviews, equally balanced among the positive and negative classes. The review lengths (after preprocessing) are in the range [1, 56], with an average review length of 20. The total vocabulary size is 18590, of which 16461 terms are available from the pre-trained word vectors (Google News data).

For the preprocessing steps, rst all HTML tags like < br/ > were removed and all text was lowercased. Then the text was tokenized, treating commas, parentheses, exclamation marks and question marks as separate tokens and ignoring periods. Also, the expression'ss, 've, 're, n't, 'd and 'll are treated as separate tokens.

### 5.2 TXT-CNN model and con guration

Our main model for text classi cation is TXT-CNN, which is a con gurable, shallow CNN with at most one hidden layer (Figure 8 represents the multichannel variant of this network, as described below). The network is based on the work of Kim [8] (the main di erence being the possibility of an additional hidden layer in our model). Arguing that the vectors that are used for input representation (i.e. word2vec) already carry word information on multiple levels of abstraction (semantically and syntactically), we did not con gure MiP-EGO to search for networks with multiple hidden layers. Furthermore, we adopt 3 variants for input representation:

Static: input word vectors from word2vec's pre-trained Google News vectors that are not updated during training;

Non-static: the input word vectors (same as above) are ne-tuned (updated) during training;

Multichannel : a combination of static and non-static, where one set of inputs is kept static and the other is ne-tuned using SGD at training time.

The network receives as input a sentence matrix (two for the multichannel architecture), followed by a dropout layer  $d_0$ . Initially, the network was designed to apply convolutional Iters of 3 sizes  $k_i$  to the input, with  $f_i$  di erent Iters per Iter size ( i 2 f 1; 2; 3g). In later experiments, we treated the number of di erent Iter sizes f as a tuneable hyperparameter of the model. The convolutions are calculated using an activation function f and with or without an additional trainable bias term f b. After global-max pooling of the resulting feature maps, the concatenated neurons are, via a dropout layer f connected to a hidden layer of sizeh, using relu activation and a bias term. Finally, the output is calculated as a linear combination of the hidden neurons and a bias term using sigmoid activation, again via a dropout layer f linear concatenated features are connected to the output via only a single dropout layer.

 $<sup>^2\,</sup>https://www.cs.cornell.edu/people/pabo/movie-review-data/$ 

Figure 8: Multichannel architecture of our main model. The con gurable hyperparameters we want MiP-EGO to learn are listed in Table 1, along with their corresponding ranges.

For all networks, the training objective is to minimize the binary cross-entropy loss function. Optimization is done using either Adam [36] or Adadelta [37], which both are widely used methods for SGD optimization. We perform early stopping whenever the loss on the test set does not improve in 15 consecutive epochs. Furthermore, we set the maximum number of epochs at 150 and we make sure to save the (up to that point) best performing model after every epoch, such that it can be loaded later for evaluation on the test set. We use 300 embedding dimensions for word2vec training of words that are not in the set of pre-trained word vectors (Google News dataset, section 2.1.2).

variable	range				
а	[elu, relu, tanh, sigmoid, selu]				
f	[1,100]				
k	[1,15]				
h	[0,100]				
S	[1, 10]				
d	[0,0.95]				
b	[True, False]				
balance	[True, False]				
model	[static, nonstatic, multi]				
optimizer	[Adam, Adadelta]				

Table 1: Tuneable hyperparameters and ranges for MiP-EGO to optimize

Variable size inputs Because all input data must have the same dimensionality, all sentence matrices were padded with zeros up to the maximum review length in the dataset (56). Because convolutions on these padding vectors take dot products of zeros they are e ectively ignored.

## 5.3 MiP-EGO con guration

Search space With the variables and corresponding ranges from Table 1 we can de ne the search space for MiP-EGO as the Cartesian product of the heterogeneous search spaces induced by the continuous),( ordinal (f, k, h and a) and nominal (all remaining) variables.

Loss function Given a con guration , MIP-EGO calculates a loss value based on the classi cation accuracy of the network on the test set. The loss function is de ned as

$$loss() = log(1 test\_accuracy)$$
 (15)

Thus, the loss is at most 0 when the accuracy on the test set is 0.0 and decreases exponentially as the test accuracy increases.

Initialization Initialization of the algorithm is done by drawing 5 points using Latin Hypercube Sampling (LHS). We set the evaluation budget for evaluating parameter con gurations at 1000.

In Il-criterion The in Il-criterion (acquisition function) that we use in our experiments is either Expected Improvement (EI), Moment-Generation Function-based In II (MGFI) or Probability of Improvement (PI).

MIES parameters Candidate points (con gurations) are selected by maximizing the in II-criterion using MIES. We used = 4 for the parent population and = 10 for the o spring population, and used an evaluation budget of 500 generational cycles.

Surrogate model We use Random Forest as our surrogate model for optimization. The number of trees is determined experimentally, as discussed in the next subsection.

### 5.4 Baseline Models and Experimental Setup

In order to compare the quality of MiP-EGO to alternative tuning methods (i.e. grid search), we rst establish two baselines. The rst is the network con guration that Kim found via grid search and tested on the same dataset [8]. We re-implemented this model and report the accuracy we found, i.e. 80.94 as opposed to the 81.5 as reported by Kim. This di erence is most likely due to the fact that di erent folds were used for the cross-validation. The second baseline model is an extension of the rst where a hidden layer was added and di erent regularization parameters were used that led to better results (this model was found after a new grid search that we performed on top of the rst baseline). The performances of these networks were measured by 10-fold cross-validation of the test accuracy. That is, 10% of the data was randomly selected as test data and the remaining 90% as training data. The folds are chosen such that all data serve exactly once as test data and are used for training in all other folds. The exact baseline network con gurations and their performance can be found in Table 2.

An important part of MiP-EGO is constructing the surrogate model (Random Forest) that is used for selecting candidate points to evaluate. We therefore rst investigate the e ect of the number of trees in our Random Forest on the search performance of our algorithm on a single fold of the data. Also, after search is completed, we use the complete dataset of sampled points for thing the Random Forest and calculate the

Parameter	Baseline 1	Baseline 2
Number of hidden neurons (0 in absence of hidden layer)	0	10
Sizes of the conv. Iters	3, 4, 5	3, 4, 5
Dropout probabilities for the dropout layers as shown in	0, 0.5, 0	0.5, 0.5, 0.8
Figure 8 (0 when the dropout layer is absent)	0, 0.5, 0	0.3, 0.3, 0.8
The number of convolutional Iters that are used per Iter size	100	100
Batch size during SGD optimization	50	50
Boolean variable for adding an additional trainable bias	VOC	
term to the computed convolutions or not	yes	yes
L <sub>2</sub> max constraint on weights when working with L2-norm	3	_
constraint regularization	3	_
Boolean variable for weighting classes inversely proportional	no	no
to their underlying class frequencies during training or not	110	110
Boolean variable for generating vectors that are not in the		
set of pre-trained w2v-vectors with word2vec on the training	no	yes
data (no means random vectors)		
Context window size for w2v training	-	10
Performance: test accuracy on 10-fold cross-validation	80.94	81.52

Table 2: Parameter con gurations for our baseline models.

# R<sup>2</sup>-score for determining the quality of the t.

In our experiments, when searching optimal network con gurations with MiP-EGO, we only evaluate network performance on one fold of the data. After completion of an optimization run using a speci c setup (number of trees in the Random Forest, acquisition function etc.), we use the 5 highest scoring con gurations that were found along the full optimization run and perform the complete 10-fold cross-validation with these con gurations (on the exact same train/test-splits as our baseline models to make comparison between di erent con gurations on the same data possible).

# 6 Results

### 6.1 El-based optimization

Figure 9 shows the test accuracy of the incumbent during optimization using Expected Improvement as acquisition function on a single fold of the data, for di erent sizes of the Random Forest. Additionally, in Table 3, the R<sup>2</sup>-scores are given for Random Forests of di erent sizes after tting them on their corresponding accumulated data set after optimization (i.e. 1000 samples), as well as the nal incumbent accuracy.

RF	Acc.(%)	R <sup>2</sup>
10	83.64	0.862
50	84.02	0.879
80	84.02	0.879
90	84.30	0.874
100	84.02	0.882
110	84.21	0.885
150	84.49	0.879

Figure 9: Test accuracies of the incumbent during El-optimization of the surrogate model for di erent sizes of the RF (on a single data fold).

Table 3: Test accuracies and R<sup>2</sup>-scores of theRF for di erent sizes.

Highest test accuracy is achieved with 150 trees in the RF, while the best model in terms of R²-score is the RF with 110 trees. Figure 10 shows the average, 10-fold cross-validated test accuracies after EI-optimization using di erent RF sizes. The gure shows the 5 highest scoring con gurations that were found in a single optimization run. Table 4 summarizes the average 10-fold cross-validated accuracies. Highest cross-validation accuracies are achieved here by the surrogate mode RF) with 110 trees.

Number of trees in the Random Forest												
	10	50	80	90	100	110	150					
cv 1	75.09	81.36	81.45	63.73	81.73	81.80	75.10					
cv 2	81.37	69.49	81.49	81.49	81.58	81.74	70.93					
cv 3	81.42	81.46	75.10	75.64	73.75	81.89	72.15					
cv 4	81.67	75.54	72.18	68.08	61.32	81.66	60.20					
cv 5	81.11	69.34	75.92	78.37	72.24	81.4	43 77.86					

Table 4: Average accuracies for 10-fold cross-validation of the 5 best con gurations after EI-optimization for di erent sizes of the surrogate model RF sizes), with accuracies that exceed our baseline in bold.

Figure 10: Cross-validated test accuracies of the 5 best con gurations after EI-optimization of the surrogate model for di erent sizes (number of estimators/trees) of the RF. The red line corresponds to our main baseline (81.52).

#### 6.2 MGFI-based optimization

Figure 11 summarizes the results for optimization using the MGFI -acquisition function on a single fold of the data. Figure 11a rst shows how the test accuracy of the incumbent changes during optimization as di erent RF sizes are used, while keeping the parameter at its default value (t=2). The corresponding  $R^2$ -scores are listed in Table 5. The results for di erent values of t (t0 in the gures) when using a forest with 110 trees are shown in Figure 11b. Finally, Figure 11c shows the e ect of using a cooling scheme for the parameter, cooling down from t = 2 to t = 0:1 and again using a forest of size 110. The nal incumbent accuracies are listed under Table 6.

For the very small set of Random Forest sizes that were tested here, a forest with 110 trees achieves the highest R<sup>2</sup>-score (Table 5). Furthermore, we see that = 2 performs best here, and that the use of a cooling schedule does not lead to better results on this single data fold. However, the di erences in performance of the optimal con gurations are very small for the di erent setups that were tested.

From Figure 11b we can partly see the in uence of thet-parameter on the convergence rate. Witht = 2 the algorithm converges the fastest whilet = 5 has the slowest convergence. The convergence rates for values of 3 and 4 for t are in between these two boundaries. Furthermore, from Figure 11c we can see that an exponential schedule leads to quicker convergence than a linear schedule.

Figure 11: Test accuracies of the incumbent for MGFI-based optimization on one fold of the data.

RF

Acq.

t0

Schedule

		80	MGFI	2	-
		100	MGFI	2	-
		110	MGFI	2	-
		110	MGFI	3	-
RF	R <sup>2</sup>	110	MGFI	4	-
80	0.877	110	MGFI	5	-
100	0.878	110	MGFI	2	lin
110	0.886	110	MGFI	2	expo

80 0.877 100 0.878 110 0.886

Table 5: R2 scores for surrogate models with di erent number of trees

Table 6: Final incumbent accuracies for one fold of the data with the optimization setups from Figure 11

Accuracy

84.02 84.58 84.02 84.02 84.30 84.21

83.93

The average 10-fold cross-validated results are also listed under Table 7, again for the 5 highest scoring con gurations that were found in a single optimization run. For the cross-validation results of the incumbents from Table 6 (rst line in Table 7), we see that the setup with an exponential cooling schedule (t0=2) performs best (81.83), closely followed by the setup with a xed t of 2 (81.81).

		trees			tO	sched.		
	80 100 110		110	3	4	5	lin.	exp.
cv 1	78.64	78.51	81.81	81.74	78.52	81.42	81.36	81.83
cv 2	81.48	81.45	81.51	81.1	5 75.5	581.54	81.21	81.36
cv 3	75.24	81.76	81.68	78.29	81.43	81.95	81.11	71.97
cv 4	75.92	72.56	81.22	81.3	681.87	81.58	81.47	72.88
cv 5	81.51	81.41	81.79	81.85	82.01	81.41	81.57	81.35

Table 7: Average cross-validated accuracies (baseline-exceeding scores in bold)

#### 6.3 PI and variable s

The remaining results are for PI-based optimization using a Random Forest with 110 trees, and optimization of a slightly modi ed version of the TXT-CNN model where the number of Iter sizes s is a tuneable hyperparameter as well (as explained in section 5.2). The latter was optimized using the EI acquisition function and again using a Random Forest with 110 trees. Figure 12 shows the test accuracies of the incumbent during optimization of these two methods for a single fold of the data. The nal incumbent accuracy is given in Table 8, as well as the average 10-fold cross-validated accuracies of the 5 highest scoring con gurations in Figure 12.

	PI	var s
fold	84.30	83.55
cv 1	81.66	81.54
cv 2	81.70	78.34
cv 3	81.36	81.45
cv 4	78.35	81.50
cv 5	81.26	81.36

Figure 12: Test accuracies of the incumbent during Ploptimization (blue line) and El-optimization with tuneable s on one fold (both with 110 trees)

Table 8: Final incumbent test accuracies from Fig. 12 (rst line) and cross-validated accuracies of the 5 best con gurations

# 6.4 Best con gurations

Table 9 summarizes which settings for MiP-EGO achieved the highest cross-validated test accuracies among all results that were previously discussed. The size of the Random Forest was 110 for all these setups. Furthermore, the outer right column speci es the rank of the con guration in the initial single-fold optimization (among the top 5 best scoring con gurations) that led to this nal cross-validated test accuracy. Table 10 shows the corresponding con gurations that were found using the settings from Table 9.

#	Acq.	t <sub>o</sub>	sched.	Fold rank
1	MGFI	5	-	3
2	EI	-	-	3
3	MGFI	4	-	4
4	MGFI	3	-	5
5	MGFI	2	exp	1

Table 9: MiP-EGO settings that led to the highest cross-validated test accuracies.

#	model	balance	a b	)	d <sub>0</sub>	d <sub>1</sub>	$d_2$	$k_0$	k <sub>1</sub>	k <sub>2</sub>	h	$f_0$	f <sub>1</sub>	$f_2$	opt. it	er c	/
0	multi	False	relu T	rue	0.500	0.500	0.800	3	4	5	10	100	100	100	Adadelta	-	81.52
1	multi	True	relu Tr	rue	0.000	0.915	0.416	4	1	2	66	41	100	6	Adadelta	640	81.95
2	multi	True	elu Tr	rue	0.374	0.811	0.002	1	2	6	2	89	5	15	Adadelta	262	81.89
3	multi	True	relu Fa	alse	0.333	0.753	0.091	5	2	1	2	2	84	56	Adadelta	71	81.87
4	multi	False	relu F	alse	0.358	0.602	0.024	1	2	1	78	73	51	64	Adadelta	161	81.85
5	multi	False	relu F	alse	0.391	0.647	0.193	4	1	2	43	11	73	69	Adadelta	446	81.83

Table 10: The con gurations that achieved the highest cross-validated test accuracies (outer right column), along with the number of iterations MiP-EGO needed to nd them. Con guration corresponds to our baseline model.

### 7 Discussion and conclusions

Using CNNs for text classi cation is a very promising approach that is completely di erent from traditional techniques for performing this task. The combination of input representation using high quality word embeddings and a network that is able to automatically extract useful features from these is a fundamentally di erent approach than using e.g. SVMs for NLP tasks, which are typically based on the Bag-of-Words model. The major shortcoming of neural networks in general, however, is that their black-box nature makes it impossible to optimize the model by hand and without expert knowledge. Even for a relatively simple network like TXT-CNN, it is extremely di cult to determine good ranges for e.g. continuous variables (i.e. dropout layers), which increase the search space dramatically, as very small changes can already lead to very di erent performances.

We have seen that automatic con guration of our TXT-CNN model using MiP-EGO is able to achieve state-of-the-art performance on our movie review dataset without using much prior knowledge. The dropout probabilities, for example, were allowed to take on values ranging from 0 up to 0.95: a range that would be impractical for a grid search (in combination with all other variables). Not only is our algorithm able to nd good solutions, it also takes away the tedious process of deciding which con gurations to prioritize when performing a grid search: after initialization, no more user input or comparison is required and we can simply work with the highest scoring con gurations that are found after optimization is completed.

Although we have only performed experiments on a single dataset where we applied a speci c (con gurable) model to a speci c problem, MiP-EGO is also a very promising method for optimizing other problems like image classi cation [12]. This makes it a very useful technique for increasing autonomy of machine learning models in general and black-box models in particular.

Limitations and future work One limitation of our approach for optimizing CNNs is that we de ne a xed search space before running the algorithm that is not able to grow dynamically. Because of this, interdependencies between conditional variables need to be taken care of manually. This is the case in our model, where we decided to use 3 di erent lter sizes, each with a di erent number of lters. We experimented with an additional masking variable s (ranging from 1 to 10) to control the number of active lter sizes in the network. In this approach, however, the initial search space is still xed, but some dimensions are simply ignored by the network during optimization (and not by MiP-EGO). Furthermore, our approach for optimizing the model on a single fold of the data and looking at cross-validation results of the highest scoring con gurations afterwards is very unlikely to nd optimal con gurations for the full cross-validation. The algorithm is prone to over thing the network in this manner. This is clearly rejected by the fact that the best con gurations that we found (Tables 9 and 10) were in 4 of the 5 cases the highest scoring con guration in the corresponding single fold experiments. An experimental setup that performs a full cross-validation at each MiP-EGO iteration is thus a better approach for exceeding the baseline as much as possible. The downside of this is obviously that the evaluation time of a speci c con guration will increase with a factor 10, but most likely fewer iterations will be needed for achieving similar (cross-validation) results.

All in all, we have seen that Bayesian Optimization (MiP-EGO) is a very elective way for optimizing CNN architecture for text classication and takes away much of the work and time that users would have to spend when designing these networks manually.

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